

CONSIDERATIONS OF SPATIAL RESOLUTION IN 3D-TV SERVICE COMPATIBLE FRAME PACKING SYSTEMS

INTRODUCTION

The need to transport 3D signals using existing HD production and distribution infrastructures has led to the development of "Dual image stereoscopic 3D imaging systems." These systems deliver two images (left eye and right eye) that are arranged to be seen simultaneously (or near simultaneously) by the left and right eyes. This mimics the natural binocular viewing experience and viewers perceive increased depth in the picture.

The "3D frame compatible packing method" is among the various methods adopted for carrying the two images of a stereo pair over existing HDTV systems. This method produces a 3D effect by combining the left and right pictures (a.k.a. "stereo pair") comprising the 3D information into a single HD frame (*spatial multiplex*). Achieving this result requires downsizing the stereo pair, squeezing¹ the frames horizontally and/or vertically.

Similar dual image stereoscopic systems were considered by the film industry. During the early "Golden Era" of 3-D cinematography of the 1950s and the second Hollywood-driven boom of 3-D films in 1983, stereoscopic motion pictures were produced through a variety of different methods. Fixing a 3D lens adapter (a.k.a. *beamsplitter*) to the lens of the film camera (35mm or 16mm) enabled the camera to direct light from two separate points (left eye and right eye points), through mirrors, and on to two separate parts of the same frame of film. Two formats were used by cinema at different times:

- "Side-by-Side" storing the left and right eye images, one beside the other in a vertical split frame, squeezing them horizontally.
- "Over-Under" storing the left and right eye images, one above the other in a horizontal split frame, squeezing them vertically.



Side-by-Side on 70mm film



Over-Under on 35mm film

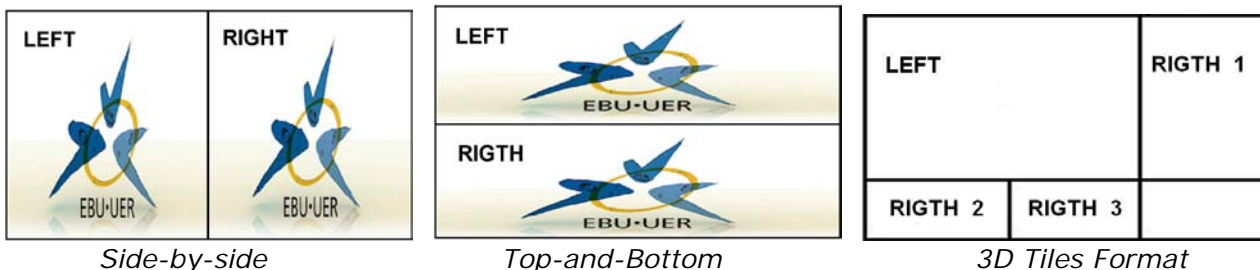
In the present day similar techniques been adopted in the push toward "service compatible 3D TV":

- "Side-by-Side" (SbS) = the left and right images are inserted one next to the other in the 720p or 1080i HD frame. This requires a horizontal squeeze of the video signal which causes halves horizontal definition.

¹ In a digital signal processing the image squeezing is performed through proper filtering, followed by a decimation in order to reduce possible aliasing. The **decimation** is a technique for reducing the number of samples in a discrete-time signal. The term comes from the Latin *decimatio* meaning "removal of a tenth" (*decem* = *ten*), a form of military discipline used by officers in the Roman Army to punish mutinous or cowardly soldiers.

- "Top-and-Bottom" (TaB) = the left and right images are inserted one above the other in the 720p or 1080i HD frame. Here, vertical squeeze is required which halves vertical definition.

- "3D-Tile Format" = two 720p images (left and right) are packed into a single 1080p frame, inserting one 720p image unchanged, that is without any downsizing, while splitting the other 720p image into three parts (tiles) and remapping the pixel location but without any filtering/decimation.



The present paper theoretically evaluates the resolution losses of these 3D HD formats in the context of the horizontal and vertical resolution of the 2D HD standards in use in Europe today and into whose frame the stereo pair is packed: 720p/50, 1080i/25, and 1080p/50.

The same argument also applies to formats adopting 59.94/60 rates.

RESOLUTION EVALUATION

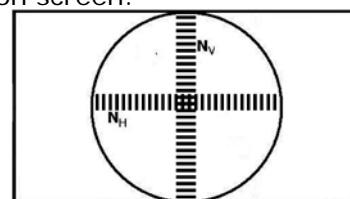
In cinema and television the term "resolution" is understood to evaluate how close picture details (ideally considered as *line pairs* formed by a dark line and an adjacent light line) can be to each other and still be visibly resolved.

In cinematography, resolution evaluation is tied to physical sizes, being specified as the "number of line-pairs per unit-distance" (LP/mm) along the vertical and horizontal axis.

In television, resolution evaluation is tied to the overall size of a picture, being specified, horizontally and vertically, by the "number of line pairs per picture height" (LPH). In particular:

- The vertical resolution N_v defines the capability of the system to resolve horizontal lines and depends primarily on the number of scanning lines per picture and the combined effects of the camera and display capabilities (Kell and Interlace effects, described in greater detail below). It is specified as the number of distinct horizontal lines pairs which can be satisfactorily resolved on the television screen.

- The horizontal resolution N_h defines the capability of the system to resolve vertical lines. It depends on the sampling frequency adopted by the system, that is on the camera and display capabilities, taking into consideration the aspect ratio (AR) of the system and the cut-off frequency of the anti-aliasing filter. It is expressed as the number of distinct vertical lines pairs, which can be satisfactorily resolved in $1/AR$ of the width of a television screen.²



² To maintain the same spatial scale for vertical and horizontal resolution, horizontal resolution is also specified as "lines per picture height" (LPH) rather than "lines per picture width" (LPW).

VERTICAL RESOLUTION

The vertical resolution would equal, only ideally, the “number of active lines” (N_{al}) per frame. This would happen only if the scanning lines of any acquisition means (camera or scanner, where the scanning line is performed by a row of sensitive cells) were centered on the picture details. Conversely, complete loss of vertical resolution will occur when the scanning spot straddles the picture details.

A loss in the vertical resolution can be signified by multiplying the number of active lines (N_{al}) by the vertical Kell factor (vKf), whose value, which can be statistically detected with progressive scanning, was between 0.6 and 0.8 for the old cathode ray sensors and displays and between 0,85 and 0,95³ for modern fixed pixel scanners (CCD, CMOS) and displays (LCD, PDP).

The value of the Vertical Resolution is therefore:

$$N_v = N_{al} \times vKf \quad [\text{lines}]$$

Another vertical resolution loss could arise, only on moving details in the image for interlaced scanning systems. Such loss is signified by the Interlace factor (I_f), described as “*the ratio of lines of resolution as perceived in a video picture produced using interlaced scan, divided by the lines of resolution as perceived in the same video picture except produced using progressive scan*” (see Ref.1). It is statistically evaluated as 0.7, by which the active lines should be multiplied to obtain the complete interlaced vertical resolution N_{vi} :

$$N_{vi} = N_{al} \times vKf \times I_f \quad [\text{lines}]$$

Note: for progressive pictures the Interlace factor value is 1.0.

HORIZONTAL RESOLUTION

The horizontal resolution would equal, only ideally, the “number of samples per active line” (N_{sa}) divided by the aspect ratio (AR). This would happen only if the cells of the sensors of the acquisition means (camera, scanner) were horizontally centred on the picture details. Conversely, complete loss of horizontal resolution will occur when the sensor cell straddles picture details. This loss is signified by the horizontal Kell factor (hKf), whose value is between 0.85 and 0.95.

The value of the Horizontal Resolution is therefore:

$$N_H = N_{sa} \times hKf / AR \quad [\text{lines}]$$

The following Table 1 summarizes the values of the vertical N_{v2D} and horizontal N_{H2D} resolution calculated for the 2D HD systems presently available.

³ From subjective data, obtained with progressive (non-interlaced) scanning, RCA engineer Raymond D. Kell found in 1934 that vertical resolution is reduced to 64% of the number of active lines. This value was later revised: to 0.7 for electron gun scanning (in analog TV) and more recently to 0.85 - 0.95, when fixed pixel scanning (e.g., CCD or CMOS) and fixed pixel displays (e.g., LCD or plasma) entered the market.

PARAMETER		unit	720p50	1080i25	1080p50
Frame rate (frames per second)		fps	50	25	50
Number of active lines per frame	N_{al}	---	720	1080	1080
Number samples per active line	N_{sa}	---	1280	1920	1920
Vertical Kell factor	vKf	---	0.90	0.90	0.90
Horizontal Kell factor	hKf	---	0.90	0.90	0.90
Interlace factor	lf	---	1.00	0.70	1.00
Vertical resolution (lines per picture height)	N_{V2D}	LPH	≈648	≈680	≈972
Horizontal resolution (lines per picture height)	N_{H2D}	LPH	≈648	≈972	≈972

TABLE 1 - Parameters of 2D HD Systems

EVALUATION OF THE H & V RESOLUTION OF THE 3DTV PICTURES

Packing 3D information comprised of two images inside a single frame is accomplished by squeezing the images horizontally (reducing the number of samples per active line N_{sa}), vertically (reducing the number of active lines N_{al}) or both.

This squeeze reduces the corresponding resolution by the following factors:

- vertical reduction factor $Vrf = \text{reduced } N_{al} / \text{original } N_{al}$
- horizontal reduction factor $Hrf = \text{reduced } N_{sa} / \text{original } N_{sa}$

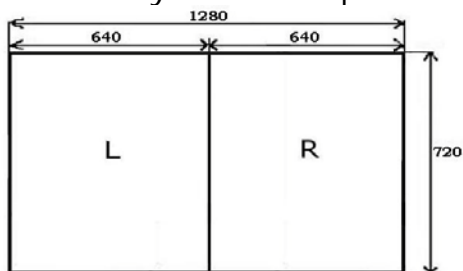
So that the H and V resolutions of the 3D left and right images are:

- 3D vertical resolution $N_{V3D} = N_{V2D} \times Vrf$
- 3D horizontal resolution $N_{H3D} = N_{H2D} \times Hrf$

Having established a baseline for 2D image resolution, the foregoing calculates the new values for the vertical resolution N_V and horizontal resolution N_H under various packing conditions adopted by the 3D industry taking into account the values of N_{V2D} e N_{H2D} of Table 1.

The values of N_V and N_H described below provide interesting insight on the performance and usability of various 3D systems.

3D SIDE-by-SIDE 720p/50



The left and right images, horizontally squeezed to a 640x720 aspect ratio, are packed side-by-side inside a 1280x720 frame and transmitted in the 720p/50 format.

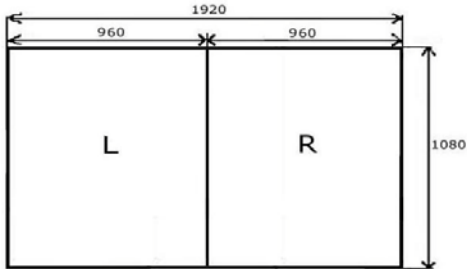
Under these conditions

$$Vrf = 720/720 = 1.0 \quad Hrf = 640/1280 = 0.5$$

and the resolution values become:

Vertical resolution $N_{V3D} = N_{V2D} \times V_{rf} = \approx 648 \times 1.0 = \approx 648$ LPH
 Horizontal resolution $N_{H3D} = N_{H2D} \times H_{rf} = \approx 648 \times 0.5 = \approx 324$ LPH

3D SIDE-by-SIDE 1080i/25



The left and right images, horizontally squeezed to a 960x1080 aspect ratio, are packed side-by-side inside a 1920x1080 frame and transmitted in the 1080i/25 format.

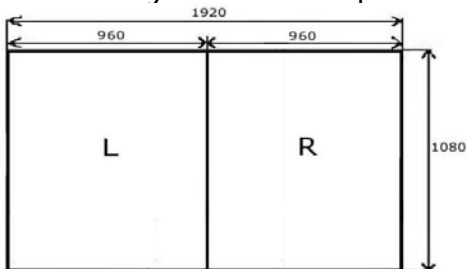
Under these conditions

$V_{rf} = 1080/1080 = 1.0$ $H_{rf} = 960/1920 = 0.5$

and the resolution values become:

Vertical resolution $N_{V3D} = N_{V2D} \times V_{rf} = \approx 680 \times 1.0 = \approx 680$ LPH
 Horizontal resolution $N_{H3D} = N_{H2D} \times H_{rf} = \approx 972 \times 0.5 = \approx 486$ LPH

3D SIDE-by-SIDE 1080p/50



The left and right images, horizontally squeezed to a 960x1080 aspect ratio, are packed side-by-side inside a 1920x1080 frame and transmitted in the 1080p/50 format.

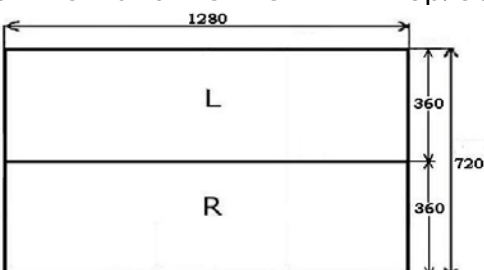
Under these conditions

$V_{rf} = 1080/1080 = 1.0$ $H_{rf} = 960/1920 = 0.5$

and the resolution values become :

Vertical resolution $N_{V3D} = N_{V2D} \times V_{rf} = \approx 972 \times 1.0 = \approx 972$ LPH
 Horizontal resolution $N_{H3D} = N_{H2D} \times H_{rf} = \approx 972 \times 0.5 = \approx 486$ LPH

3D TOP-and-BOTTOM 720p/50



The left and right images, vertically squeezed to a 360x1280 aspect ratio, are packed "top-and bottom" inside a 1250x720 frame and transmitted in the 720p/50 format.

Under these conditions

$$V_{rf} = 360/720 = 0.5$$

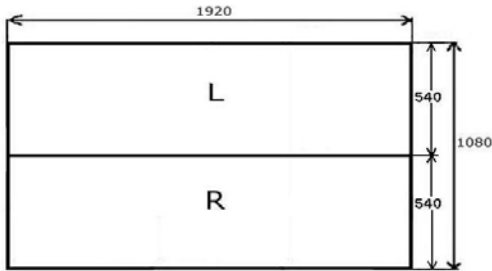
$$H_{rf} = 1280/1280 = 1.0$$

and the resolution values become:

Vertical resolution $N_{V3D} = N_{V2D} \times V_{rf} = \approx 648 \times 0.5 = \approx 324$ LPH

Horizontal resolution $N_{H3D} = N_{H2D} \times H_{rf} = \approx 648 \times 1.0 = \approx 648$ LPH

3D TOP-and-BOTTOM 1080i/25



The left and right images, vertically squeezed to a 1920x540 aspect ratio, are packed "top-and bottom" inside a 1920x1080 frame and transmitted in the 1080i/25 format.

Under these conditions

$$V_{rf} = 540/1080 = 0.5$$

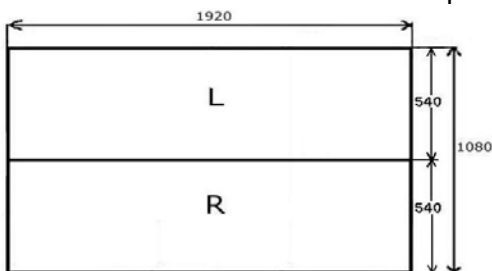
$$H_{rf} = 1920/1920 = 1.0$$

and the resolution values become:

Vertical resolution $N_{V3D} = N_{V2D} \times V_{rf} = \approx 680 \times 0.5 = \approx 340$ LPH

Horizontal resolution $N_{H3D} = N_{H2D} \times H_{rf} = \approx 972 \times 1.0 = \approx 972$ LPH

3D TOP-and-BOTTOM 1080p/50



The left and right images, vertically squeezed to a 1920x540 aspect ratio, are packed "top-and bottom" inside a 1920x1080 frame and transmitted in the 1080i/25 format.

Under these conditions

$$V_{rf} = 540/1080 = 0.5$$

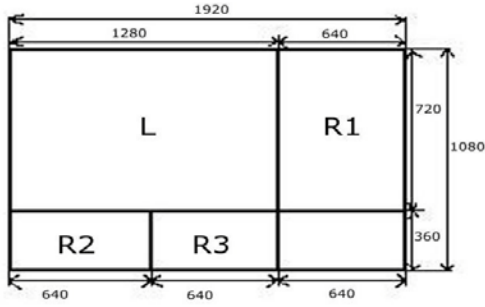
$$H_{rf} = 1920/1920 = 1.0$$

and the resolution values become:

Vertical resolution $N_{V3D} = N_{V2D} \times V_{rf} = \approx 972 \times 0.5 = \approx 486$ LPH

Horizontal resolution $N_{H3D} = N_{H2D} \times H_{rf} = \approx 972 \times 1.0 = \approx 972$ LPH

3D TILE FORMAT 1080p/50



The left and right images, both in the 720p/50 format, are packed inside a 1920x1080 frame and transmitted in the 1080p/50 format. The squeezing process is replaced by a much safer re-mapping process which eliminates image degradation problems.

The left image is inserted in the upper left part of the 1920x1080 frame while the right image is split into three tiles inserted in the remaining space of the 1920x1080 frame.

Under these conditions, the reduction factors become

$$V_{rf} = 720/1080 = 0.67 \quad H_{rf} = 1280/1920 = 0.67$$

and the resolution values become:

$$\begin{aligned} \text{Vertical resolution} \quad N_{V3D} &= N_{V2D} \times V_{rf} = \approx 972 \times 0.67 = \approx 651 \text{ LPH} \\ \text{Horizontal resolution} \quad N_{H3D} &= N_{H2D} \times H_{rf} = \approx 972 \times 0.67 = \approx 651 \text{ LPH} \end{aligned}$$

CONCLUSIONS

The following Table 2 summarizes the values of the vertical N_V and horizontal N_H resolution calculated for the 2D and 3D HD systems presently available. The \approx sign reminds us that the resolution values are strongly dependent on the values attributed to the "Kell factors" (horizontal and vertical) and to the "Interlace factor", (a source of ongoing debate since their discovery by Raymond D. Kell in 1934).

Whether the human eye is more sensitive to horizontal resolution or to vertical resolution is hotly contested in the literature, the evaluated data presented in the Table 2 for the SbS and TaB formats denounce a relevant divergence between the two types of resolution which could induce the viewers to detect a global reduction of the resolution in the reproduced images.

PARAMETER	units	2D formats			3D formats						
		720p50	1080i50	1080p50	SbS 720p50	SbS 1080i25	SbS 1080p50	TaB 720p50	TaB 1080i25	TaB 1080p50	3D Tile 1080p50
Frame rate (frames per second)	fps	50	25	50	50	25	50	50	25	50	50
Number of active lines per frame N_{al}	---	720	1920	1920	720	1080	1080	720	1080	1080	720
Number of samples per active line N_{sa}	---	1280	1920	1920	1280	1920	1920	1280	1920	1920	1280
Vertical resolution (lines per picture height) N_v	LPH	≈ 648	≈ 680	≈ 972	≈ 648	≈ 680	≈ 972	≈ 324	≈ 340	≈ 486	≈ 651
Horizontal resolution (lines per picture height) N_H	LPH	≈ 648	≈ 972	≈ 972	≈ 324	≈ 486	≈ 486	≈ 648	≈ 972	≈ 972	≈ 651

TABLE 2 - Vertical and Horizontal Resolution in 2D and 3D Systems

REFERENCES

1. Allan W. Jayne, Jr., "Video and Scanner Resolution -- The Kell Factor", www.cockam.com/kell.htm, 1997-2000
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